



Glued Joints

Keywords: trigonometry, trigonometric functions, right triangle

In this article, we demonstrate practical uses of trigonometric functions and the relationships between the lengths of the sides in a right triangle.

We focus on the topic of glued joints – connections made using adhesive materials. We show how to break down the force acting in a joint into components, distribute it across a larger area, and determine the resulting stress in the joint. We will calculate how stress changes in a slanted joint of a bar, if the bar is loaded by an axial force, compared to a perpendicular joint, as ilustrated in the figure.

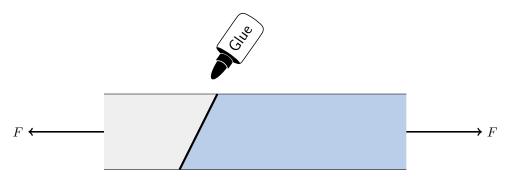


Figure 1: A slanted joint increases the resistance to stress

Types of Glued Joints and Their Stress

Everyone is familiar with joining materials by gluing. When the strength of the resulting connection is not critical, gluing is one of the simplest ways to join materials. In practice, however, we often need the joint to be both durable and strong. This means the joint should not fail when subjected to significant loading by forces. In engineering, glued joints are also referred to as bonded joints.

Adhesives (glues) typically guarantee resistance to normal stress (tensile forces) and shear stress (sliding forces), as long as stresses do not exceed the values specified by the adhesive's manufacturer.

Stress refers to mechanical pressure, defined as the ratio of the applied force to the area over which the force acts. In the case of normal stress, the force acts perpendicular to the surface. In the case of shear stress, the force acts parallel to the joint surface. The deformations caused by these forces are shown on the left: "Tensile" illustrates normal stress from perpendicular force, while "Shear" illustrates shear stress from parallel force.







Results matter!

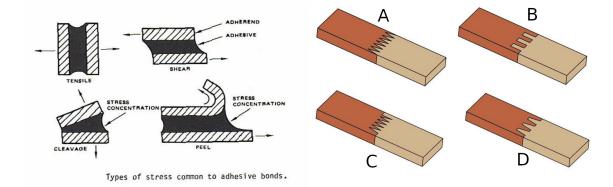


Figure 2: Left: black-and-white picture shows the types of stresses in glued joints. Top left - normal stress (Tensile), top right - shear stress (Shear). Right: the picture shows methods that allow the applied stress to be spread over a larger area and distributed into multiple components

The strength of a joint depends on the adhesive used and the materials being joined. Manufacturer data may look as follows:

- A joint glued with Loctite 421 (a superglue) has a strength of 18 MPa to 26 MPa on steel and 5 MPa to 20 MPa on polycarbonate.
- A wooden joint glued with Herkules (a dispersion adhesive) can withstand 8 MPa of shear stress.
- A joint glued with MAMUT Glue has tensile strength of 2.18 MPa and shear strength of 1.40 MPa.

Since stress in a joint is calculated as the ratio of the force to the area, one effective way to reduce stresses is to decompose the force into multiple directions and spread it over a larger area. On the right side of the previous picture, examples are shown. In joint B, the front faces are subjected to normal stress, while additional faces are loaded by pure shear stress.

We will pay special attention to slanted joints, where the connection is subjected to both normal and shear stresses simultaneously. In practice, slanted joints are often implemented differently than in Figure 1. A greater slant increases the joint strength but also takes up more space. That's why slanted joints are usually built with interruptions, rotated layers, and stacked alignment of glued segments.



Figure 3: Practical realization of a slanted joint. The beam is divided into layers with alternating slanted cuts and all parts are stacked in alignment.



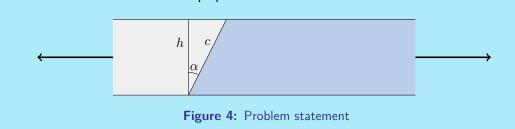




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Stress in a Slanted Joint

Task 1. Consider a bar with height $h=3\mathrm{cm}$ and width $b=4\mathrm{cm}$, glued together from two pieces along a slanted joint as shown in the figure. The angle between the joint plane and the plane of a cross-section perpendicular to the axis of the bar is $\alpha=30^\circ$. The bar is subjected to an axial force F=1~000 N. Calculate the normal and shear stresses in the slanted joint and compare them with the normal stress in the cross-section perpendicular to the axis.



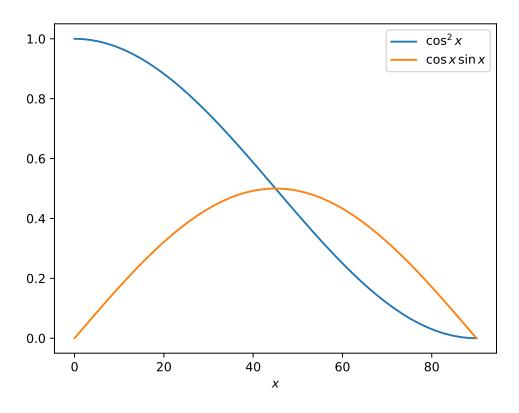


Figure 5: The graphs of functions $\cos^2 x$ and $\cos x \sin x$ for x in degrees. These functions indicate the ratio in which the stress in the joint in the bar is divided into normal and shear components







Supplementary exercises

Problem 2. Determine the angle of the slanted joint (as described in Problem 1) for which the shear stress is maximal. Also determine the corresponding normal stress.

Problem 3. The adhesive guarantees that the joint can withstand a normal stress of 10 MPa and shear stress of 8 MPa. What is then the maximum force that can be applied to the slanted joint described in Problem 1? How would the answer to this question change if the joint was slanted at an angle of 45° ?

Concluding remarks

Stresses in the plane of the connection

We have studied the forces that try to break the joint by normal stresses acting perpendicularly to the joint and shear stresses acting in the plane of the joint. In addition, the force action can still stretch the joint as a whole in the plane of the joint. In the above analysis, we were not interested in this component. However, it can be obtained from the formula for the normal stress σ_N by rotating by 90 degrees.

Defect analysis

Stress decomposition into pre-selected directions is also used in other engineering practice situations than bonding. For example, if there is an internal defect in a stressed material, knowledge of the stresses in various planes will allow to assess the risk of further propagation of this defect. In this case it is natural to transform the mechanical stresses into the direction of the defect in the same way that we transformed into the direction of the joint.

Mechanical modelling of composite materials

It is appropriate to transform the mechanical stresses into the predefined directions even when studying the deformation of composite materials. This includes both artificial composites or natural composites. Artificial composites include fiber-reinforced materials. Natural composites include the most widely used structural material, wood. These composites have different properties in different directions and when studying behavior of these materials under mechanical load it is easier to study separately the stresses in the directions related to the structure of this composite. For example, the stresses in the direction of the stiffening fibers in artificial composites, or stresses in the longitudinal direction for wood. In general, we study the stresses in the axes or planes of symmetry of the material and in directions perpendicular to these planes, in the, so called, principal directions. The response of the material to loads in the principal directions is known. The response to loads in other directions can be determined by decomposing the stresses into the individual principal directions, determine the corresponding deformations and transform this information back to obtain the final material response. Engineers know this technique as the so-called tensor transformation and have a number of techniques to solve problems of this type quickly and







Results matter!

efficiently.

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